

Distances between phylogenetic time trees

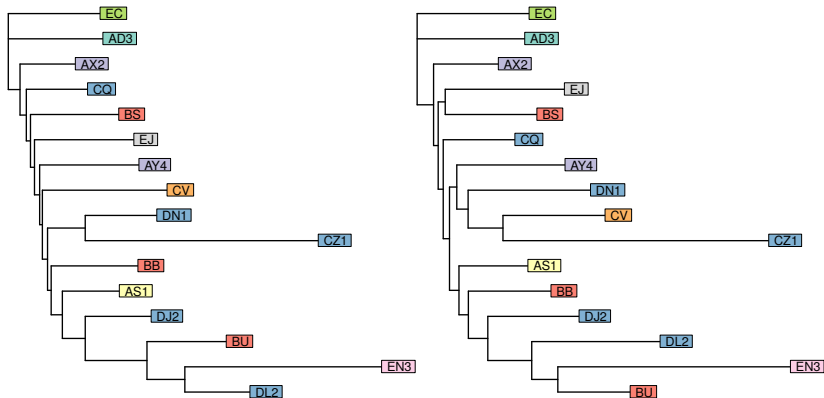
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Time trees



■ Breast

■ Thyroid

■ Lung (main tumour)

■ Pancreas

■ Vertebra C2

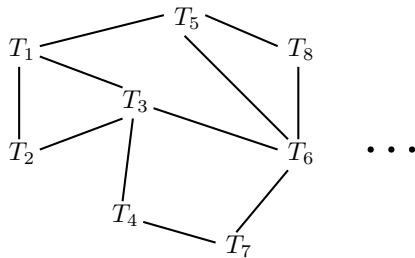
■ Kidney

■ Lung lesion

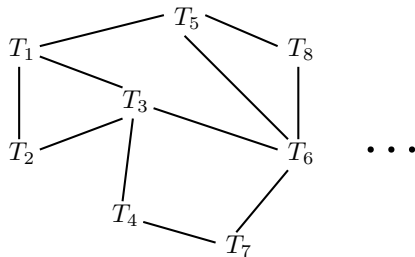
■ Eye

■ Brain

Discrete Tree Space

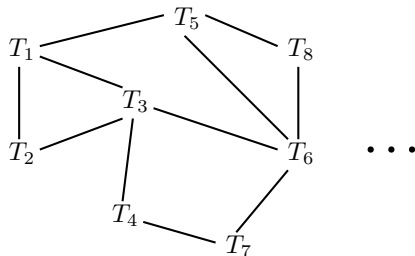


Discrete Tree Space



Popular tree re-arrangement operations: NNI, SPR, TBR

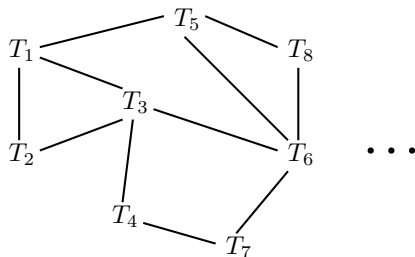
Discrete Tree Space



Popular tree re-arrangement operations: NNI, SPR, TBR

- ▶ Similarity measure

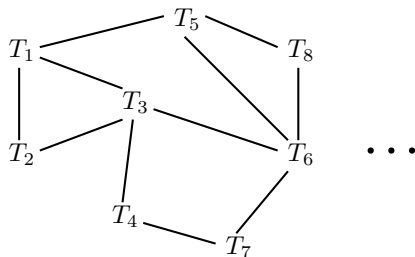
Discrete Tree Space



Popular tree re-arrangement operations: NNI, SPR, TBR

- ▶ Similarity measure
- ▶ Tree search algorithms

Discrete Tree Space



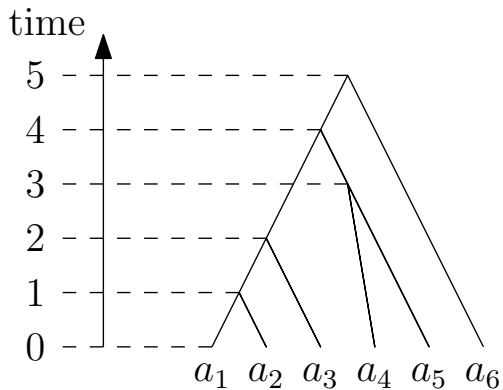
Popular tree re-arrangement operations: NNI, SPR, TBR

- ▶ Similarity measure
- ▶ Tree search algorithms

Problem: Computing distances is \mathcal{NP} -hard

Discretising Time Trees

Ranked trees

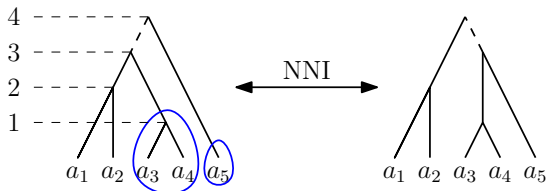


RNNI – Ranked Nearest Neighbour Interchange

NNI Move

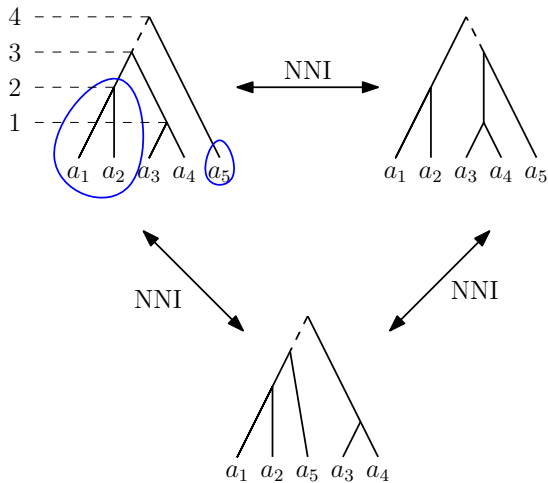
RNNI – Ranked Nearest Neighbour Interchange

NNI Move



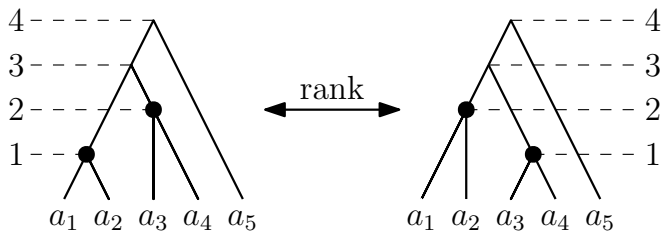
RNNI – Ranked Nearest Neighbour Interchange

NNI Move

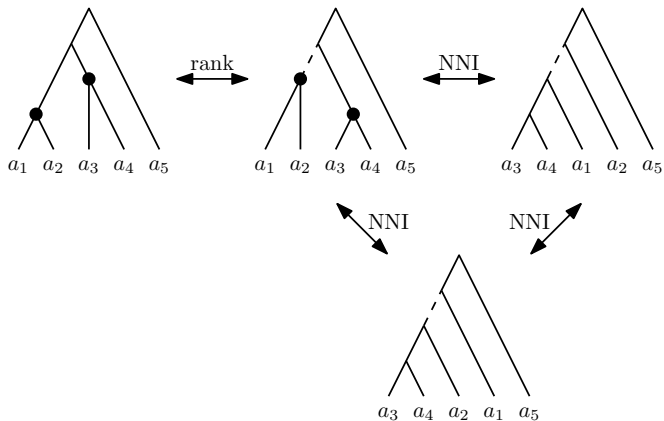


RNNI – Ranked Nearest Neighbour Interchange

Rank Move



RNNI – Ranked Nearest Neighbour Interchange

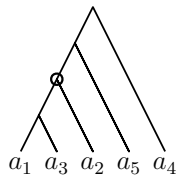
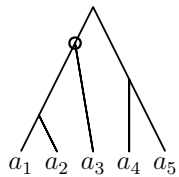


Computing shortest paths

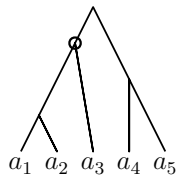
Theorem

Shortest paths in RNNI can be computed in time $\mathcal{O}(n^2)$.

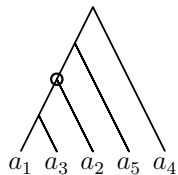
Clusters



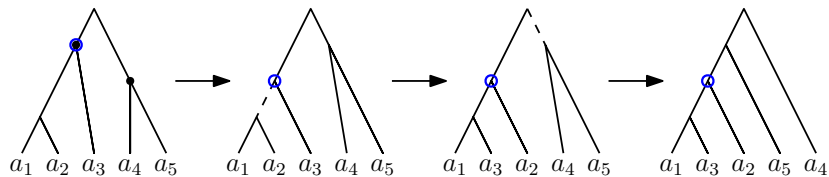
Clusters



shared cluster: $\{a_1, a_2, a_3\}$

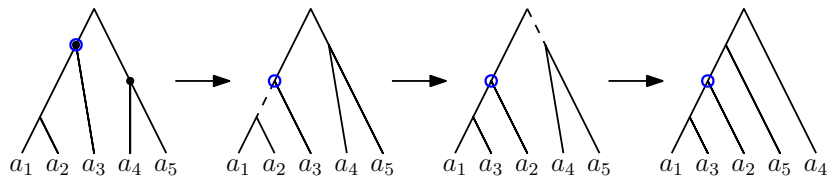


Clusters



shared cluster: $\{a_1, a_2, a_3\}$

Clusters

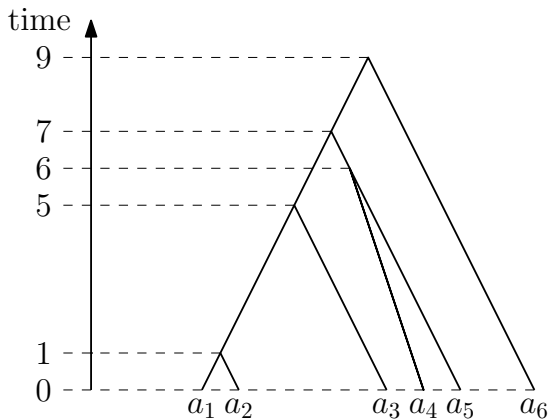


shared cluster: $\{a_1, a_2, a_3\}$

Theorem

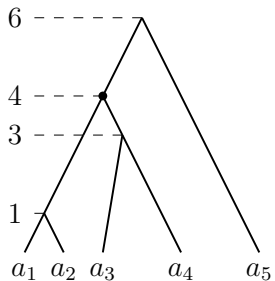
RNNI has the cluster property, i.e. a cluster shared by two trees T and R is present in every tree on every shortest path between T and R .

Discrete Coalescent Trees



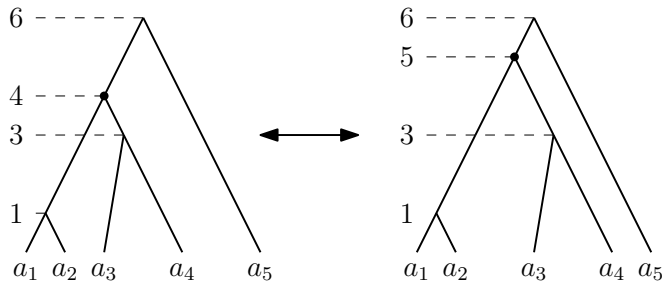
Discrete Coalescent Trees

Length moves



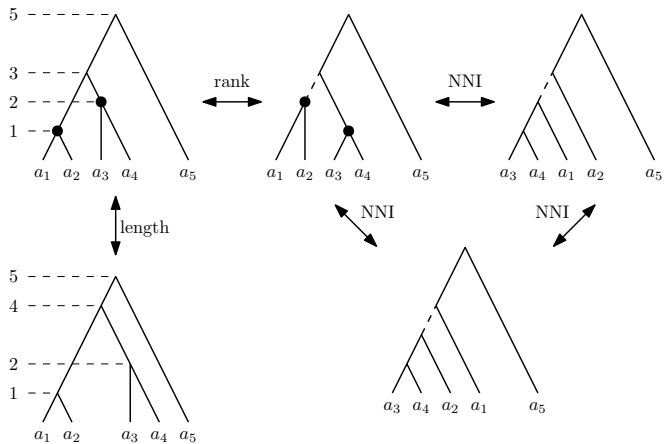
Discrete Coalescent Trees

Length moves



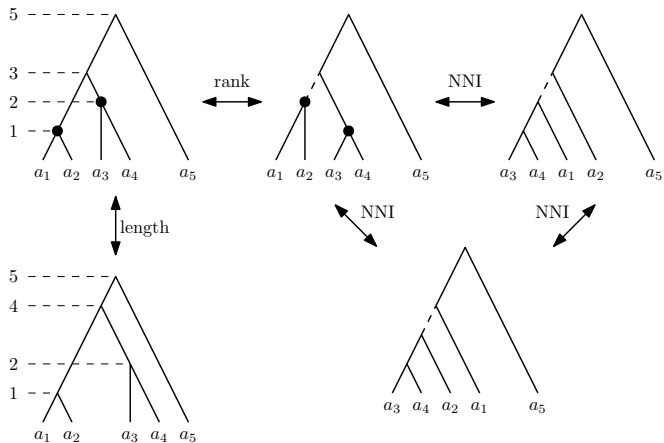
Discrete Coalescent Trees

DCT_m



Discrete Coalescent Trees

DCT_m



Parameters: n = number of leaves, m = max root time

Discrete Coalescent Trees

DCT_m – The space of discrete coalescent trees

Theorem

Shortest paths in DCT_m can be computed in $\mathcal{O}(nm)$.

Discrete Coalescent Trees

DCT_m – The space of discrete coalescent trees

Theorem

Shortest paths in DCT_m can be computed in $\mathcal{O}(nm)$.

Theorem

DCT_m has the cluster property.

Thank you

- ▶ Alex Gavryushkin (University of Otago)
- ▶ David Bryant (University of Otago)
- ▶ BioDS lab (University of Otago/Canterbury)