

The Space of Discrete Coalescent Trees

Lena Collienne

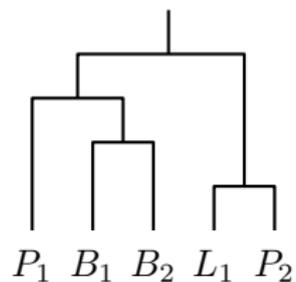
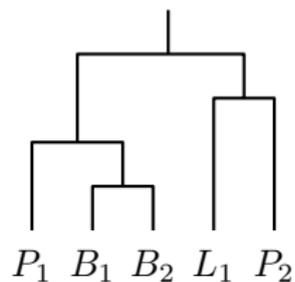


Biological Data Science Lab
Department of Computer Science
University of Otago

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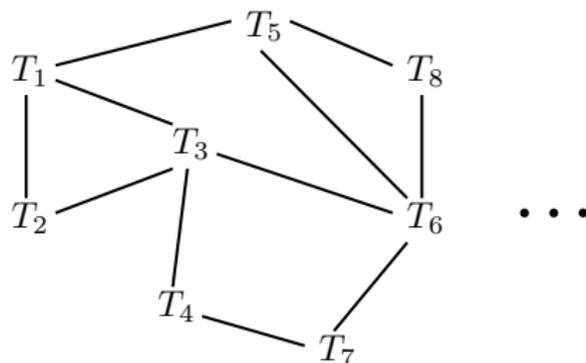
Time-trees

time ↑



- ▶ B: Brain
- ▶ P: Pancreas
- ▶ L: Lungs

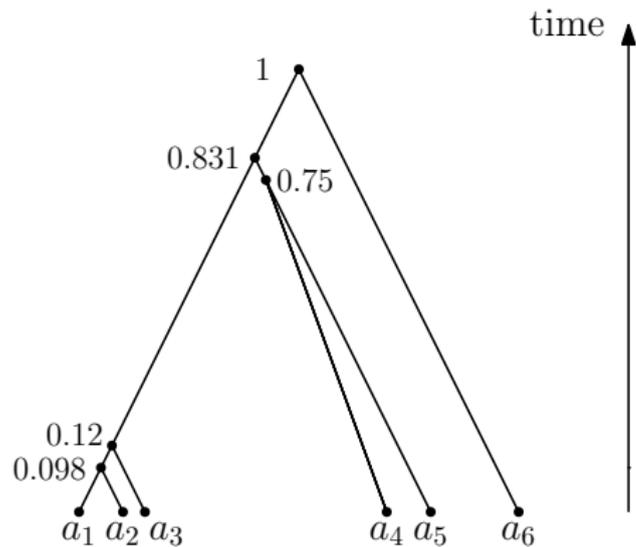
Tree Spaces



- ▶ Similarity measure for proposing trees
- ▶ Summarising trees
- ▶ ...

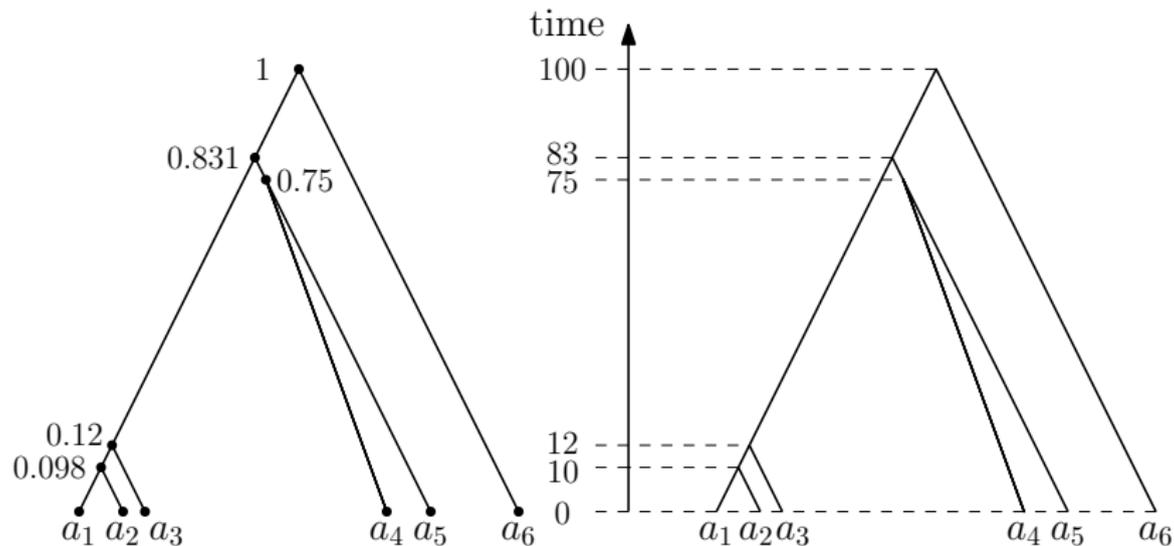
⇒ Tree re-arrangement operations (NNI, SPR, TBR)

Discretising Time Trees



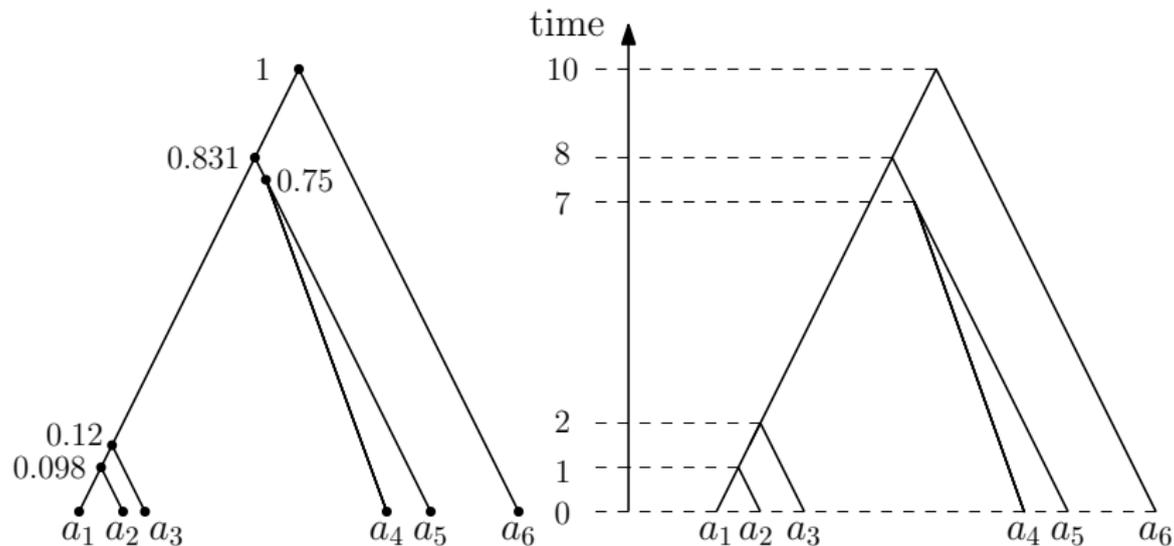
Discretising Time Trees

Discrete Coalescent Trees



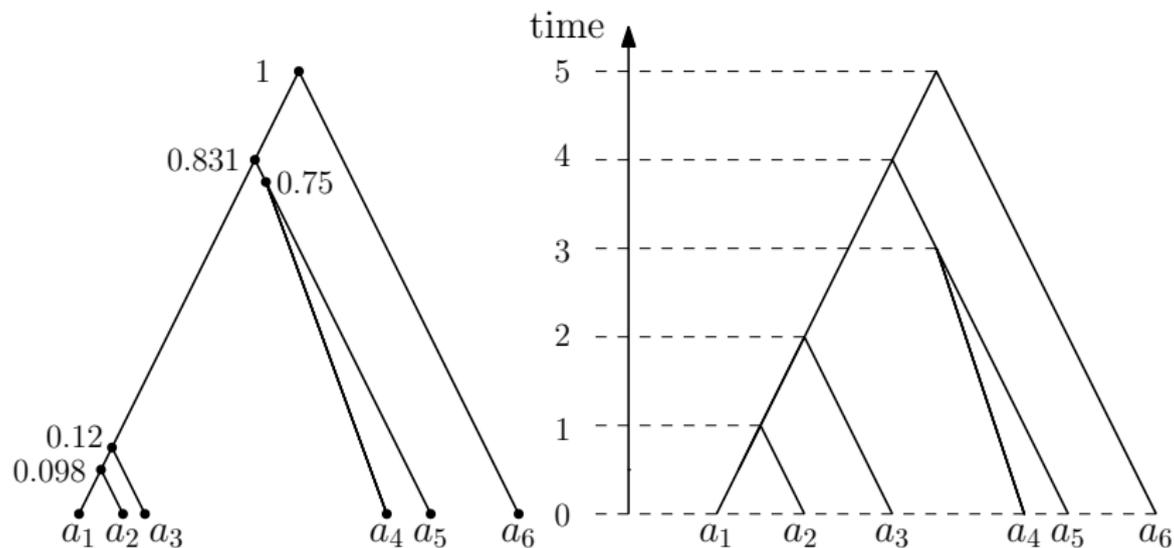
Discretising Time Trees

Discrete Coalescent Trees

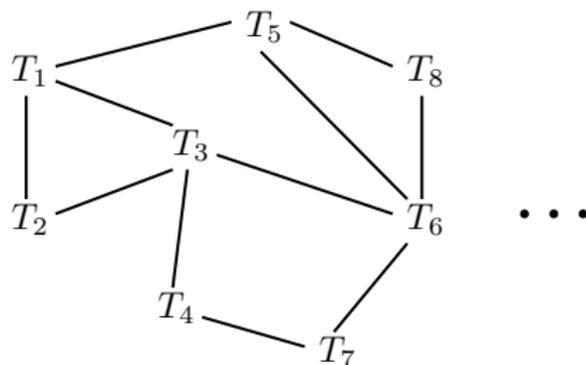


Discretising Time Trees

Ranked trees



DCT

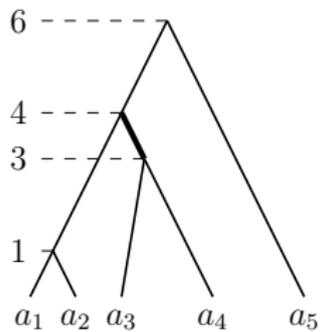


Three tree re-arrangement operations:

- ▶ NNI moves
- ▶ rank moves
- ▶ length moves

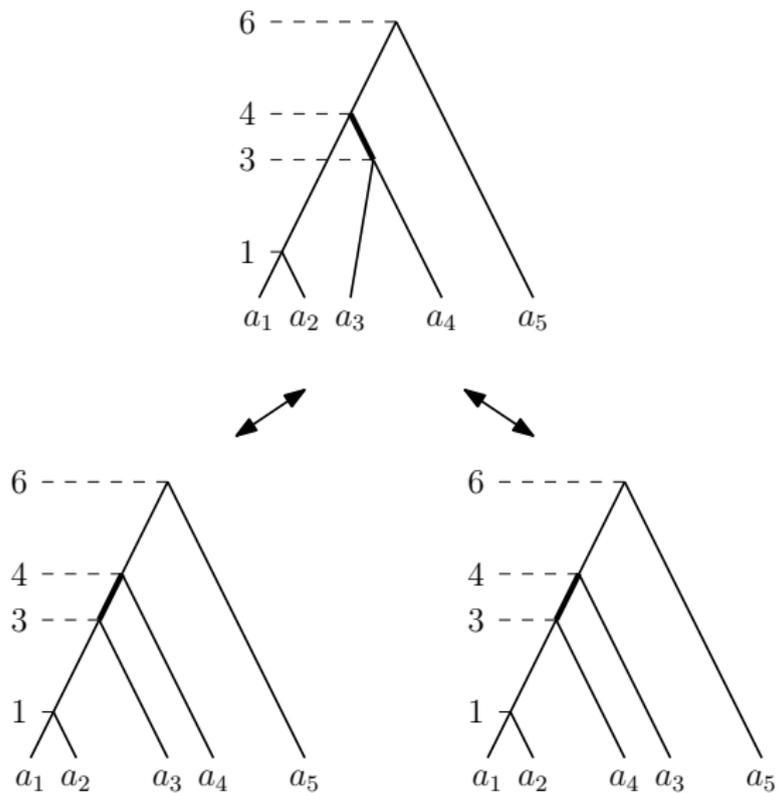
DCT

NNI Move



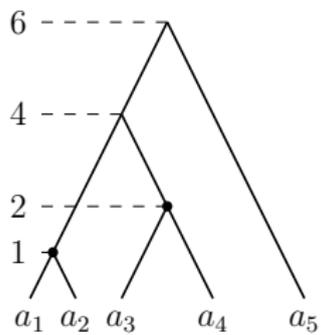
DCT

NNI Move



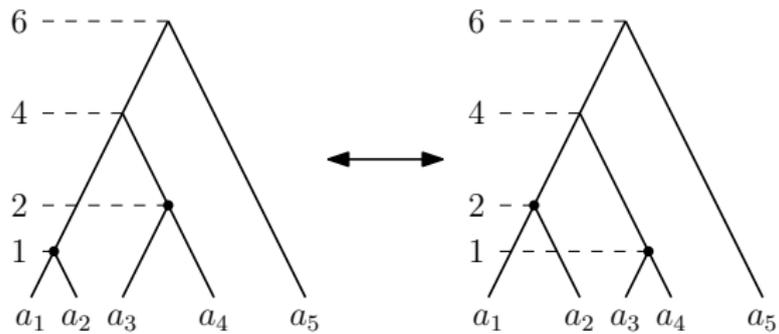
DCT

Rank Move



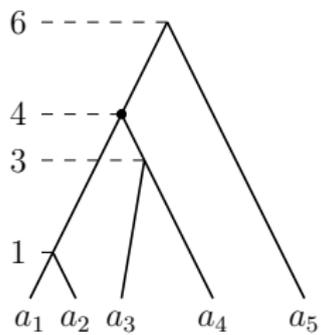
DCT

Rank Move



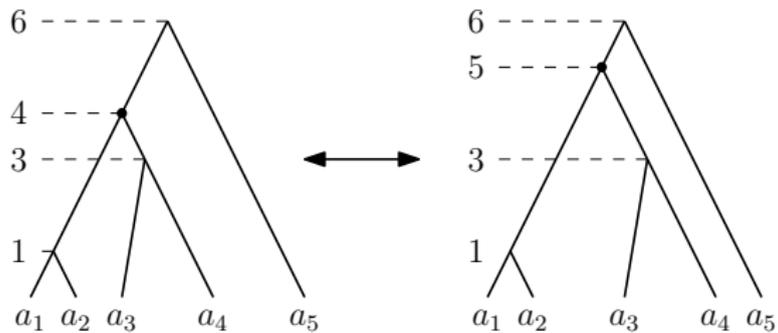
DCT

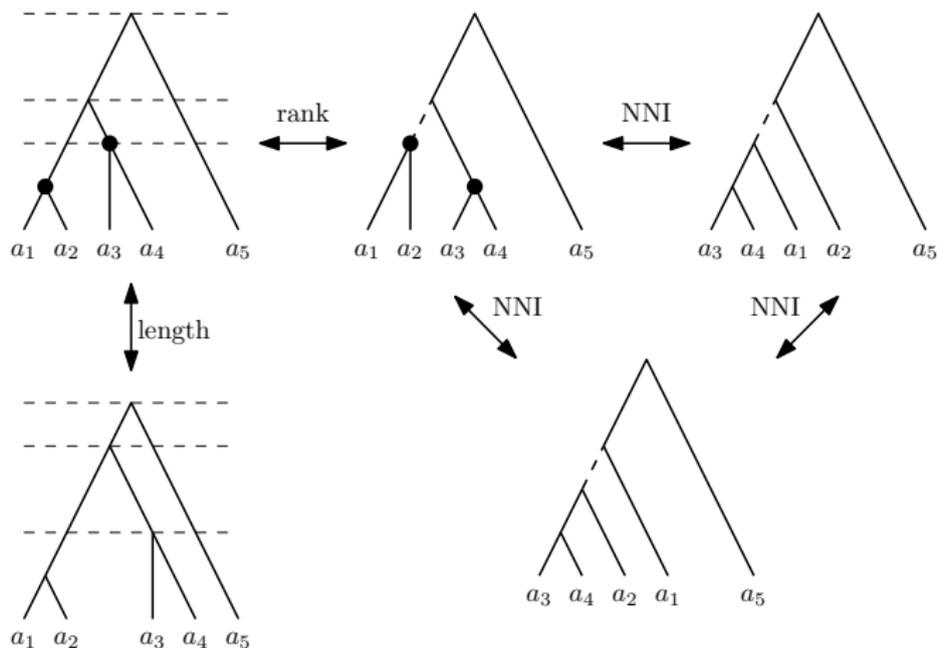
Length Move



DCT

Length Move

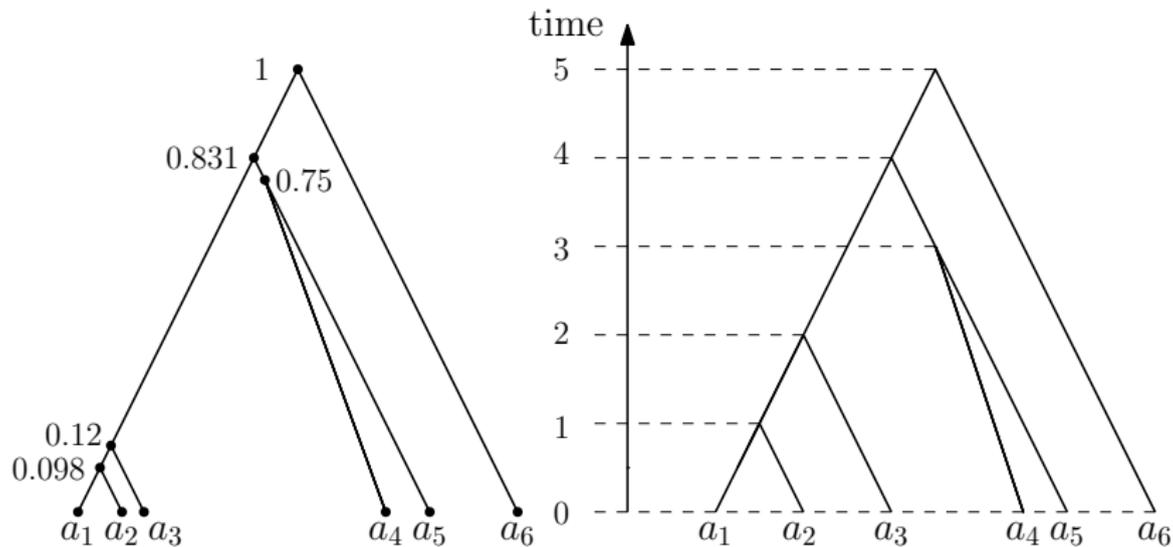




Parameters: n = number of leaves, m = max root time

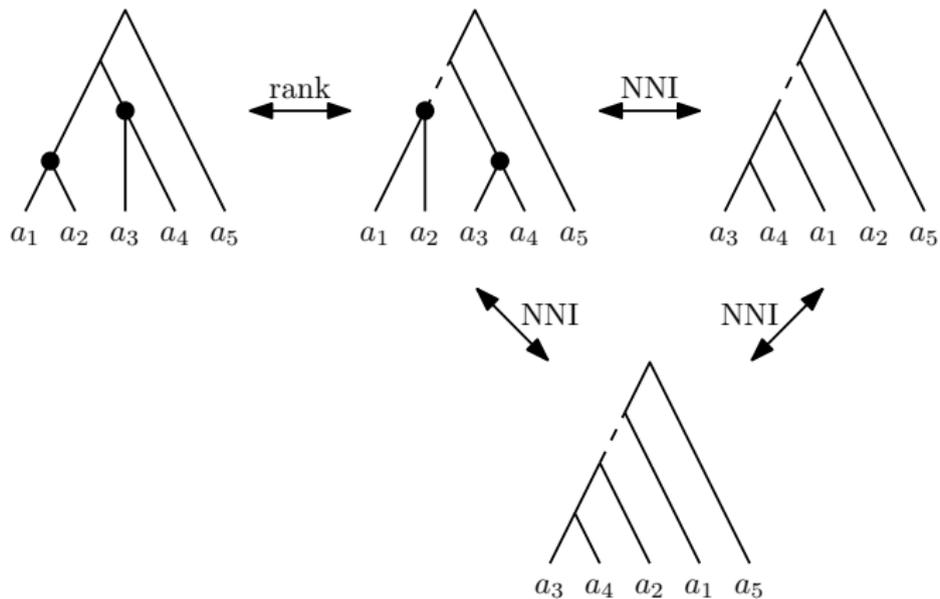
DCT_m

Special case: $m = n - 1$



DCT_{n-1}

RNNI



Computing shortest paths

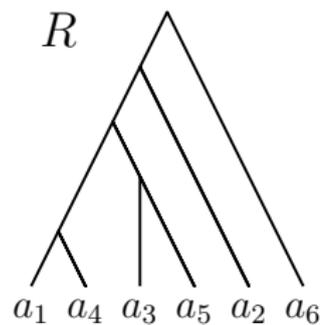
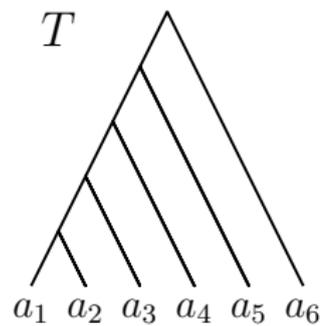
RNNI

Theorem

The algorithm FINDPATH computes shortest paths in RNNI in time $\mathcal{O}(n^2)$.

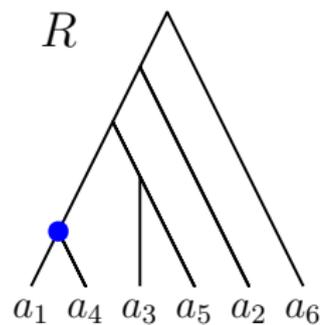
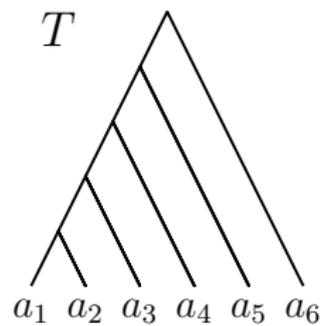
FINDPATH

RNNI



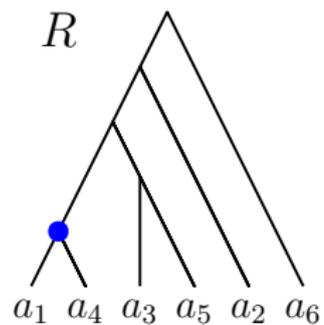
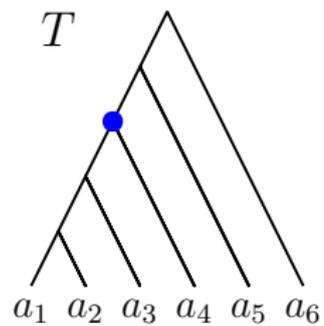
FINDPATH

RNNI



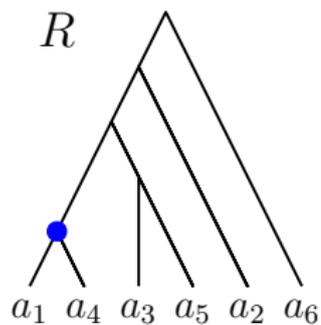
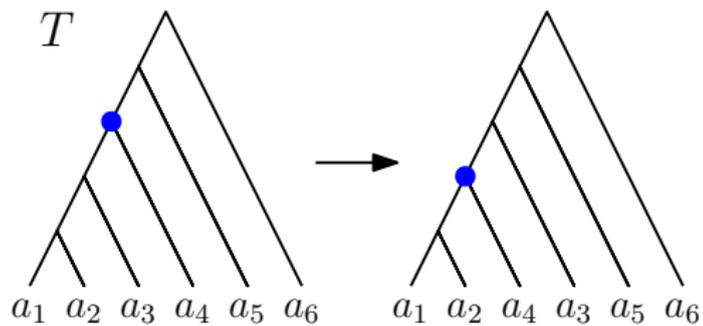
FINDPATH

RNNI



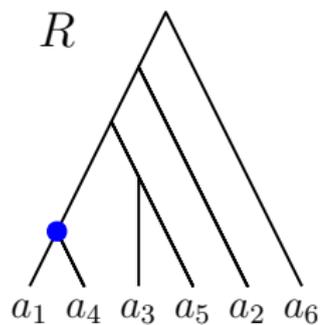
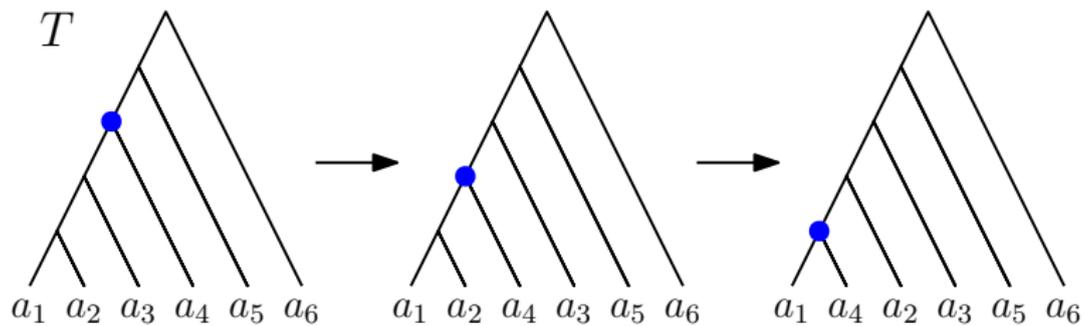
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RNNI



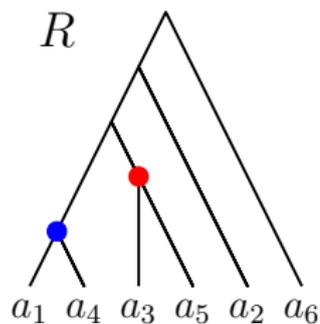
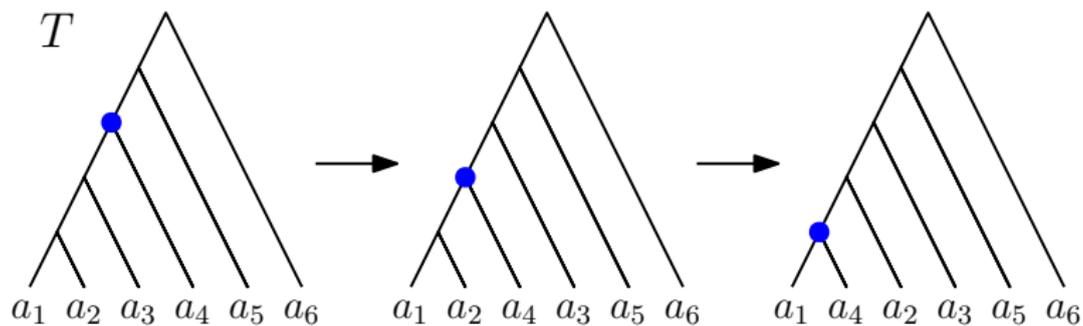
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RNNI



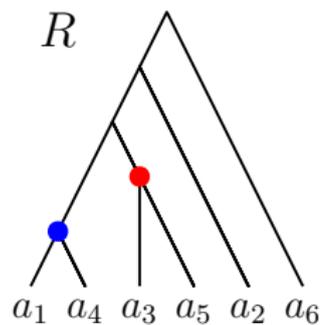
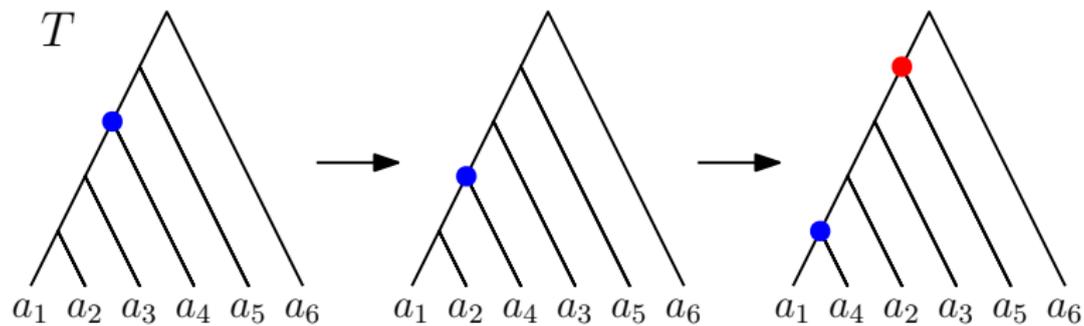
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RNNI



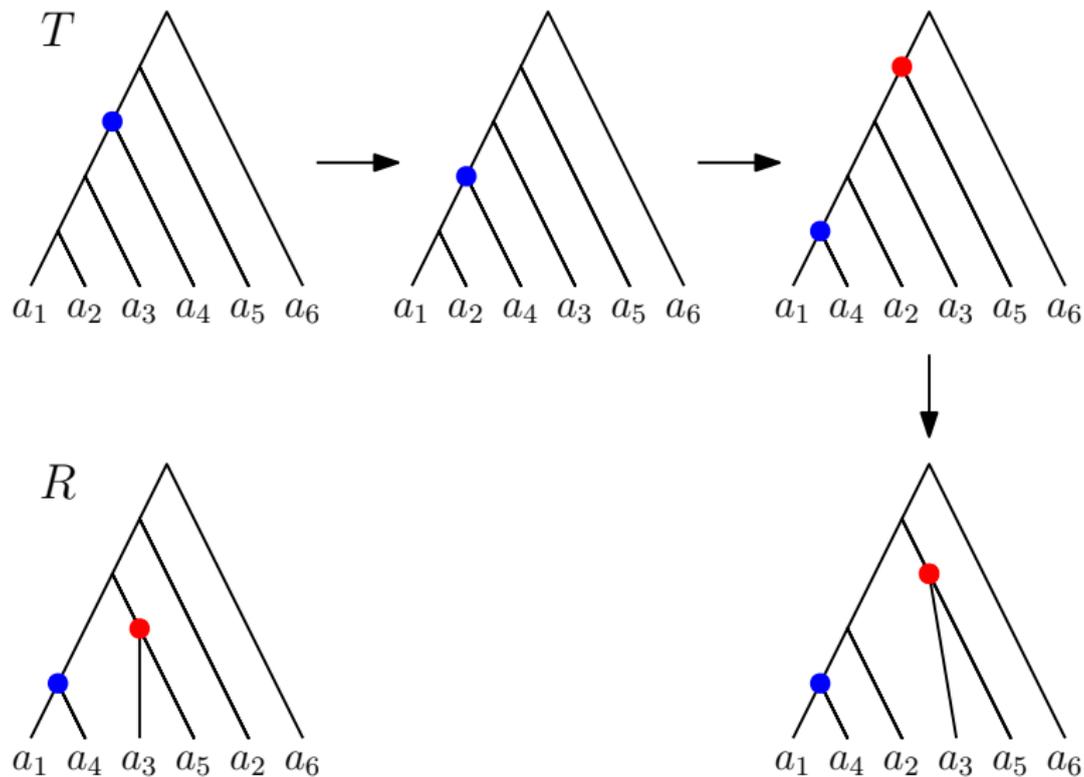
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RNNI



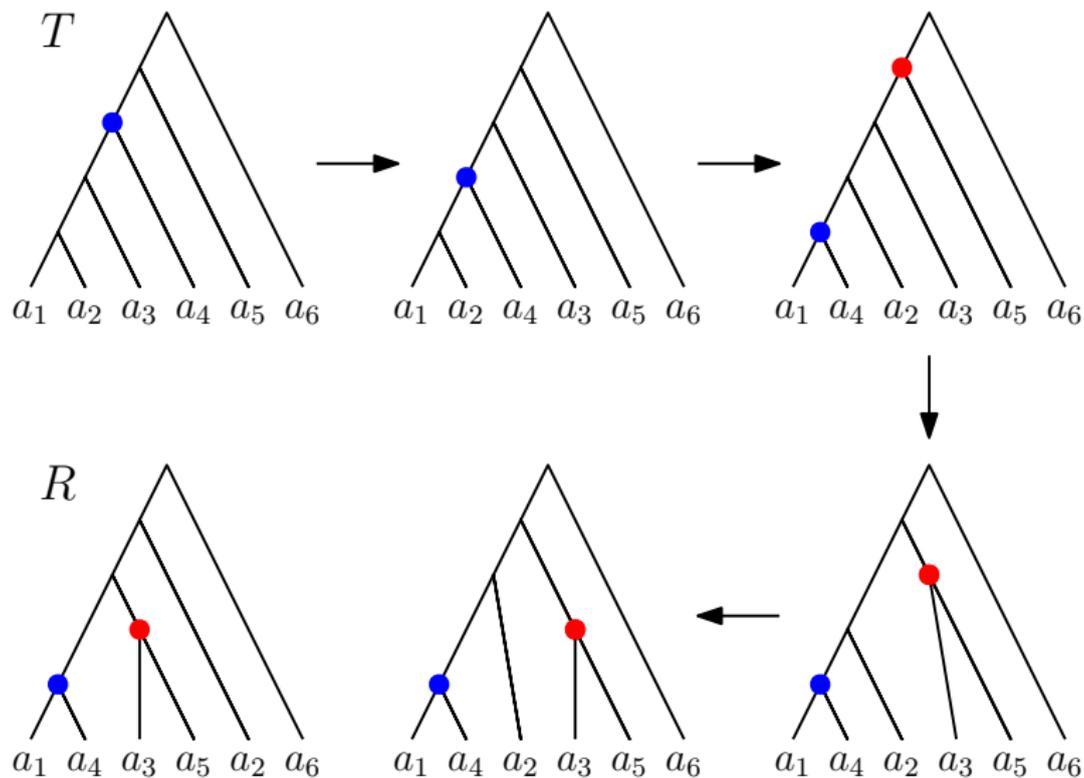
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RNNI



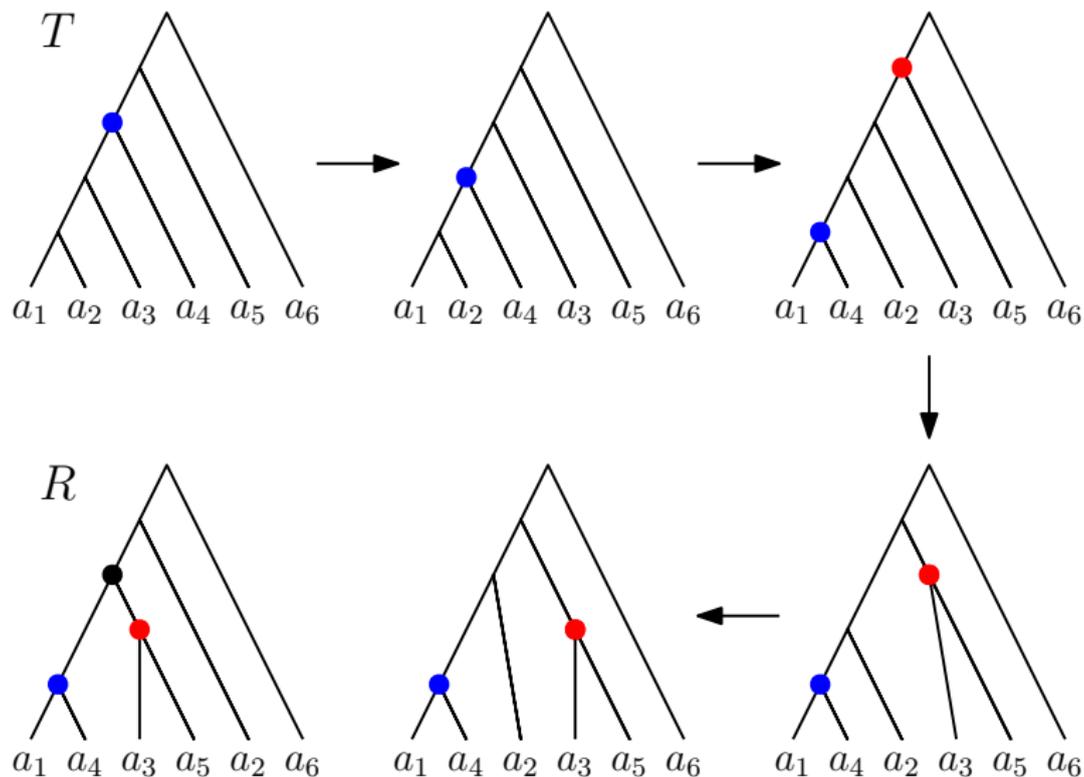
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RNNI



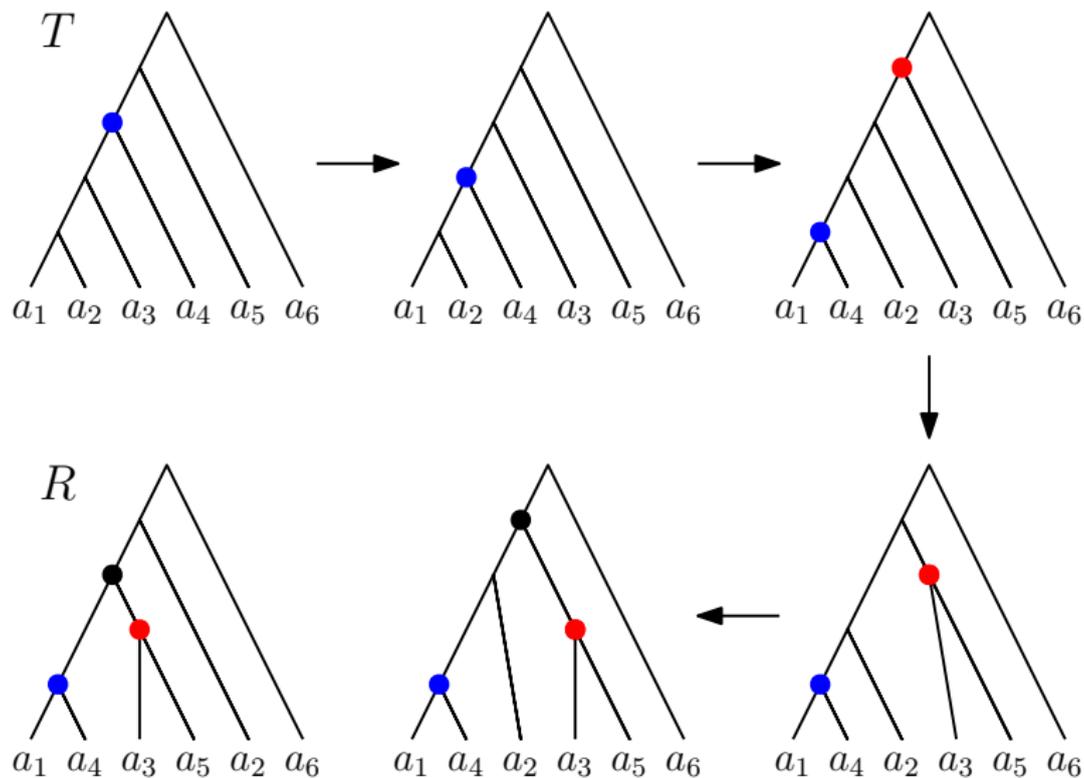
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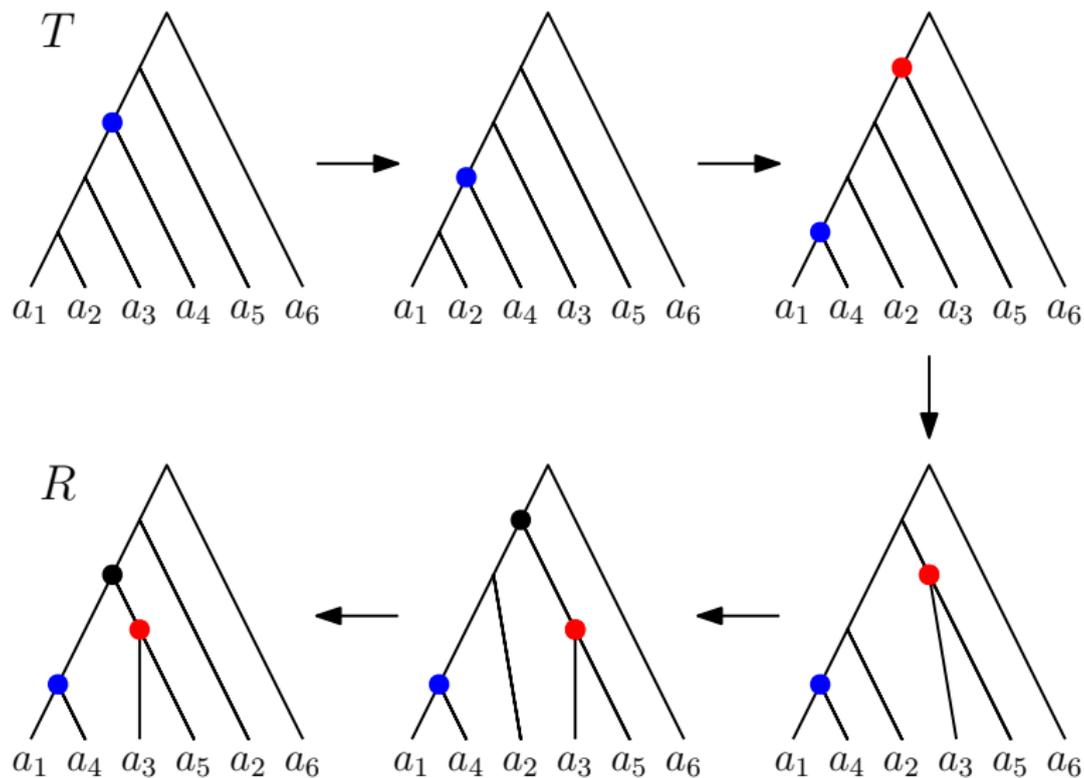
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RNNI

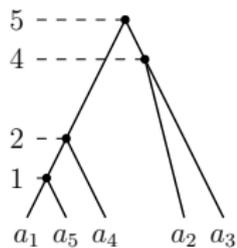
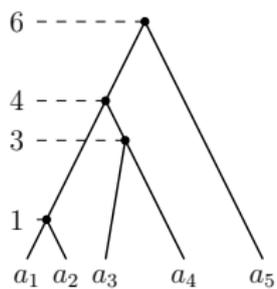


FINDPATH

RNNI

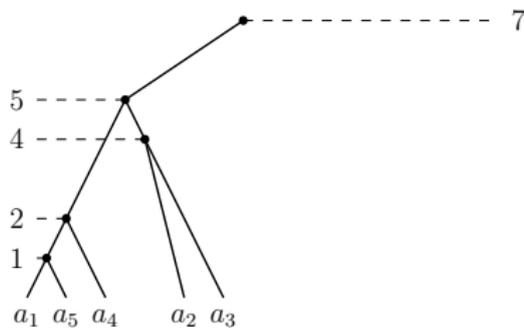
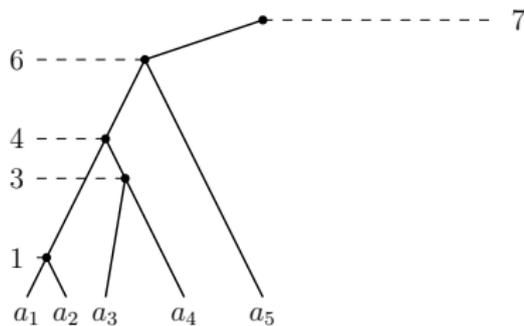


FINDPATH in DCT_m



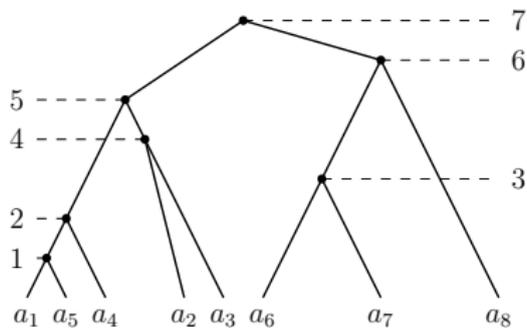
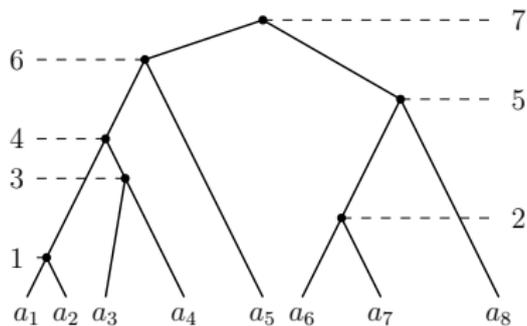
$\Rightarrow m = 6$

FINDPATH in DCT_m



$\Rightarrow m = 6$

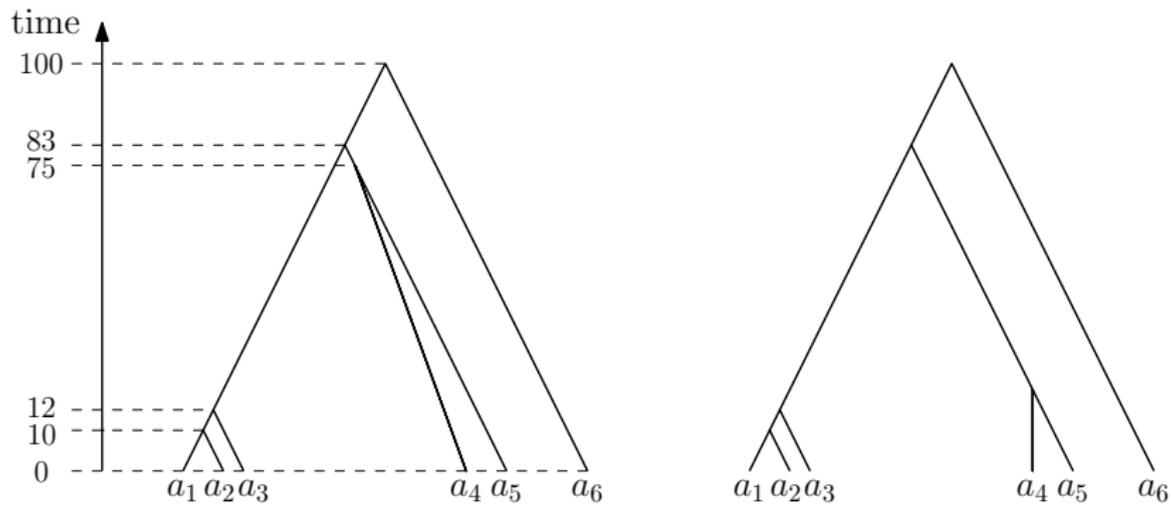
FINDPATH in DCT_m



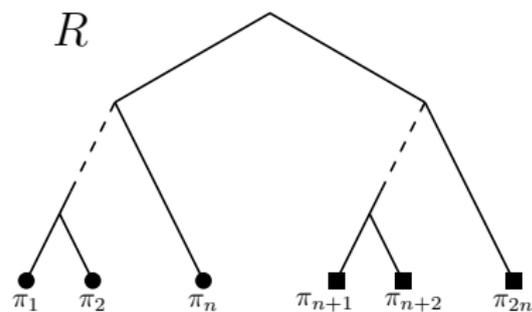
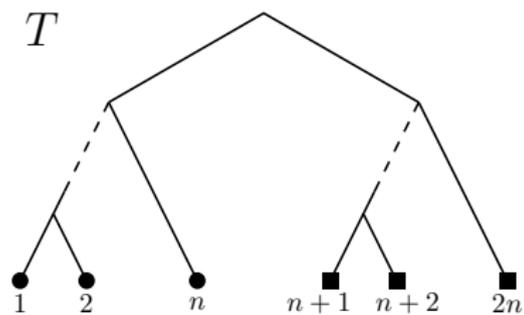
$\Rightarrow m = 6$

FINDPATH

A note on scalability



Cluster Property

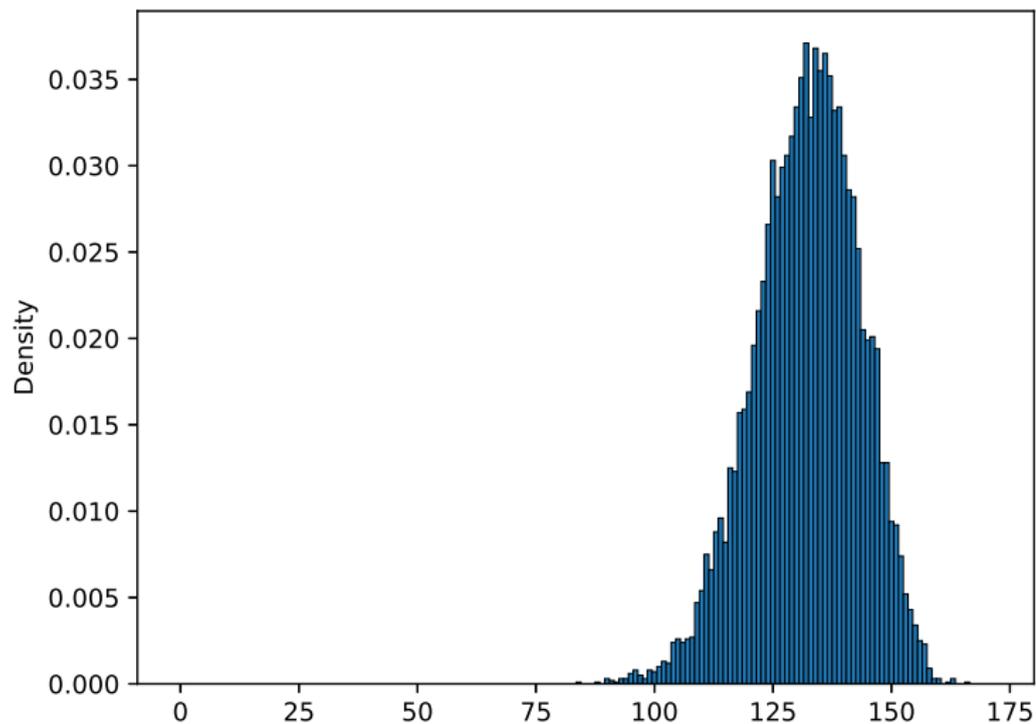


Theorem

DCT_m has the cluster property.

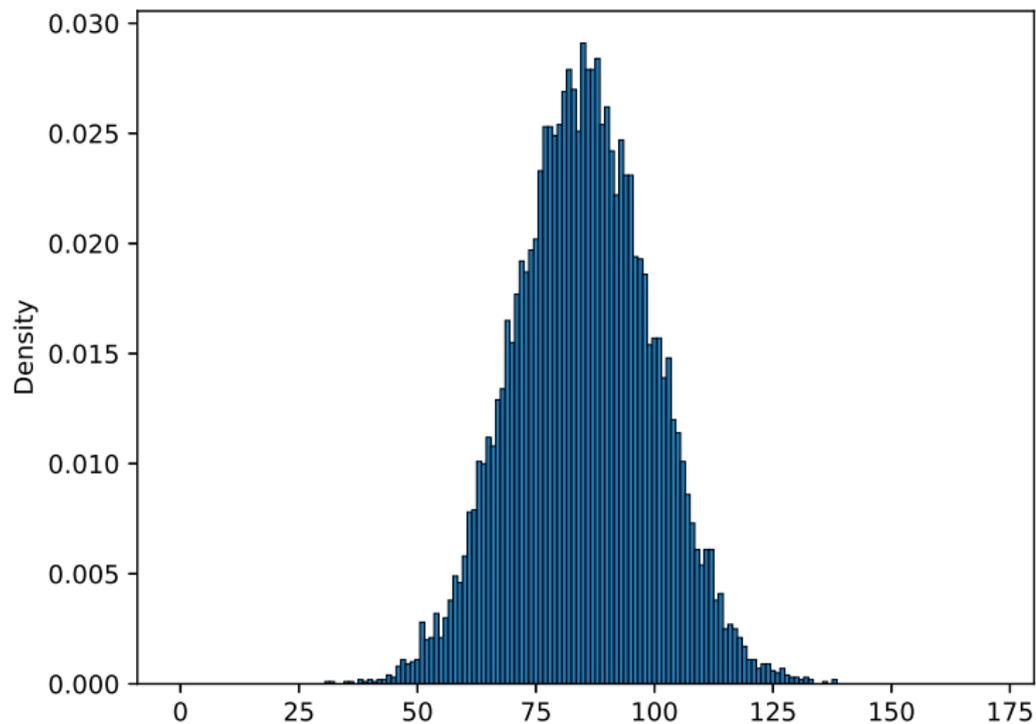
Distributions of distances

Coalescent



Distributions of distances

Birth-Death



Thank you

- ▶ Alex Gavryushkin (University of Otago)
- ▶ David Bryant (University of Otago)
- ▶ Mareike Fischer (University Greifswald)
- ▶ BioDS Lab:

